Flanking Fractures and the Formation of Double Ridges on Europa

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31 ABSTRACT

32 Europa, a satellite of Jupiter, is one of the most intriguing worlds in the solar system. Its dearth of impact craters and plethora of surface morphologies point to a dynamic evolution of its 33 34 icy shell in geologically recent times. Double ridges are a common landform and appear to have 35 formed over a significant fraction of the satellite's observed geologic history. Thus. 36 understanding their formation is critical to unraveling Europa's history, and many models have 37 been proposed to explain their creation. A clue to the formation of ridges may lie in evidence for 38 flexure of the lithosphere in response to a load imposed by the ridge itself (marginal troughs and 39 subparallel flanking fractures). When this flexure has been modeled, a simple elastic lithosphere 40 has typically been assumed; however, the generally thin lithospheres suggested by these models 41 require very high heat flows that are inconsistent with Europa's expected thermal budget (of order 1 W m⁻² vs. of order 10 mW m⁻²). Each of the proposed formational models, however, 42 43 predicts a thermal anomaly that may facilitate the flexure of Europa's lithosphere. Here, we 44 simulate this flexure in the presence of these anomalies, as a means to evaluate the different 45 models of ridge formation. We find that nearly all models of double ridge formation are 46 inconsistent with the observation of flexure (specifically the flanking fractures), except for a cryovolcanic model in which the growing ridge is underlain by a cryomagmatic sill that locally 47 48 heats and thins the lithosphere.

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50 Key Words: Geophysics; Tectonics; Jupiter, satellites; Europa

51 **1. Introduction**

52 Europa, a satellite of Jupiter, is one of the most intriguing worlds in the solar system. Only 53 slightly smaller than the Moon, Europa possesses a metallic core and a rocky mantle surrounded 54 by a shell of water/water ice ~ 100 km thick (Anderson et al., 1998; Schubert et al., 2009). Its 55 dearth of impact craters and plethora of surface morphologies point to a dynamic evolution of its 56 icy shell in geologically recent times (e.g., Greeley et al., 2004; Schenk et al., 2004; Bierhaus et 57 al., 2009). In addition, the preponderance of evidence points to a liquid water ocean beneath the 58 ice shell (e.g., Pappalardo et al., 1999; Kivelson et al., 2000). Because liquid water is a 59 necessary (but insufficient) biological requirement, Europa is one of the prime candidates for 60 extraterrestrial life in the solar system. This ice shell is of order 10 km thick (see Schenk and 61 Turtle, 2009), but regardless of whether the shell is somewhat thinner or thicker, the heat flow 62 coming out of Europa is likely greater than what can be supplied by radiogenic heating in the 63 silicate portion (see, e.g., Schubert et al., 2004; Ruiz, 2005; Sotin et al., 2009). This fact 64 implicates tidal dissipation as the engine that drives Europa's diverse (and ongoing?) activity.

65 Ridges are the most ubiquitous landform on Europa, with multiple generations of ridges cross-cutting each other (for reviews, see Pappalardo et al., 1999; Greeley et al., 2004; Prockter 66 and Patterson, 2009). These features can run remarkably uniformly for more than 1000 km 67 68 across the surface, a challenge for any model of their formation. A wide spectrum of 69 morphologies has been classified as ridges on Europa, from isolated troughs to ridge complexes 70 that display a series of subparallel features (Head et al., 1999). The most common form is 71 known as the double ridge (Fig. 1); these features are generally $\sim 0.5-2$ km wide, $\sim 100-300$ m 72 tall, and possess a central trough and outer flanks with slopes typically $< 20^{\circ}$ (Head et al., 1999; 73 Coulter et al., 2009; Coulter and Kattenhorn, 2010). These shallow angles on the outer flank are

74 usually interpreted as less than the angle of repose, suggesting non-granular processes are at 75 work. On the other hand, materials can display a wide range of repose angles, including down to $\sim 10^{\circ}$, depending on the size, shape, and stickiness of the particles (e.g., Zhou et al., 2002), as 76 77 well as the gravity of the target body (Kleinhans et al., 2011). The outer flanks of double ridges 78 appear to be dominated by mass-wasting processes. Head et al. (1999) reported that the terrain 79 immediately peripheral to a ridge can be traced up the flank of the ridge, suggesting that the 80 ridges represent upwarping of the pre-existing terrain. This interpretation, however, is not 81 unique (Sullivan et al., 1998); if ridges formed by deposition of material on the surface, they 82 would reflect to some degree the topography of the underlying terrain. Furthermore, some of the 83 cracks that persist up the flanks could be due to reactivation along pre-existing structures. A 84 subtle marginal trough a few tens of meters deep is fairly common (see Hurford et al., 2005), and 85 subparallel, presumably tensile fractures can sometimes be found near the outer reaches of these 86 troughs (Fig. 1). Additionally, the marginal troughs can sometimes possess diffuse regions of 87 lower albedo, suggesting burial or processing of the terrain.

88 Several models have been proposed for the formation of double ridges (to be reviewed in the 89 next section). All of these models appeal to exploitation of a pre-existing crack in the ice shell of 90 Europa. Addressing the source of the initial crack has been beyond the scope of these models 91 (and continues to be so in this current work), but it is thought that the cracks form in response to 92 externally applied stresses (Greeley et al., 2004; Kattenhorn and Hurford, 2009). As pointed out 93 by Greeley et al. (2004), "each model has different implications for the presence and distribution 94 of liquid water at the time of ridge formation." Given that ridges are the most ubiquitous 95 landform, it is therefore critical to understand ridge formation in order to decipher Europa's 96 unique history.

97 A clue to the formation of ridges may be provided by evidence for flexure of the lithosphere 98 in response to a load imposed by the ridge itself. Several groups have interpreted the presence of 99 marginal troughs and subparallel flanking fractures associated with ridges as characteristic of 100 flexure (e.g., Pappalardo and Coon, 1996; Tufts, 1998; Billings and Kattenhorn, 2005; Hurford et 101 al., 2005; Dombard et al., 2007). The addition of a ridge to the surface will cause the lithosphere 102 to warp downward, producing marginal troughs and uplifting a flexural bulge peripheral to these 103 troughs that may be detectible. Between the bulge and the trough, tensile flexural stresses peak 104 and may produce subparallel fractures (arrows in Fig. 1). When this flexure is modeled, a simple 105 elastic lithosphere has usually been assumed (see Turcotte and Schubert, 2002); however as we 106 will discover below, the generally thin lithospheres indicate very high heat flows inconsistent 107 with Europa's expected thermal budget, which implicates a localized thermal anomaly in the 108 formation of the double ridges (cf. Dombard et al., 2007).

109 In this paper, we will evaluate models of double ridge formation by determining which ones 110 are consistent with the observation of flexure. As we will discuss, ridges that display evidence of 111 flexure (marginal bulges, troughs, and fractures) are common but not abundant, and those that 112 possess evidence of flexure can provide important constraints. Because the bulge and trough 113 topography is subtle, we will specifically look to see which models, and under what conditions, 114 predict tensile stresses that peak at the right range of distances away from the central ridge axis, 115 and thereby are able to reproduce the flanking fractures. In the next section, we review the 116 various models that have been proposed and discuss the thermal anomalies that may be 117 associated with each one. Then, we discuss a suite of measurements of double ridges, in order to 118 determine the range of distances of the flanking fractures. We subsequently describe our 119 thermal-mechanical finite element simulations, present our results, and discuss the implications.

120 2. Models of Double Ridge Formation

121 Many of the proposed models for double ridge formation are summarized in Fig. 2. In the 122 volcanic model of Kadel et al. (1998), a pre-existing crack provides a pathway for fissure 123 eruptions that build the ridges cryoclastically (Fig. 2a). In the tidal squeezing model of 124 Greenberg et al. (1998), daily tidal forces cause the crack to open and close, squeezing material 125 onto the surface (Fig. 2b). A dike intrusion model (Turtle et al., 1998) posits that injection of 126 melt into the subsurface can deform the lithosphere around the crack, uplifting the ridge. An ice 127 wedging model (Melosh and Turtle, 2004; Han and Melosh, 2010) represents a hybrid between 128 the tidal squeezing and dike intrusion models. Here, water fills a crack that opens during the 129 tensile part of a tidal cycle but does not reach the surface because of enhanced cooling; the 130 subsurface build-up of ice wedges open the crack and deforms the surface, producing the ridge. 131 Head et al. (1999) proposed that the crack leads to formation of a wall diapir of warm ice that 132 uplifts the ridge (Fig. 2c), while Sullivan et al. (1998) argued that the ridge represents a 133 symmetric buckle of the lithosphere adjacent to the crack under a compressive stress state (Fig. 134 2d). A shear heating model (Gaidos and Nimmo, 2000; Nimmo and Gaidos, 2002; Han and 135 Showman, 2008) has been proposed where cyclical strike-slip motion on a crack dissipates heat 136 in the interior, resulting in the warmer, buoyant ice uplifting the ridge (Fig. 2e).

Last, Dombard et al. (2007) recently proposed a variant of the cryovolcanic model. In volcanic systems on Earth, the amount of subsurface magmatism generally exceeds the amount of surface volcanism, often by a large amount (Crisp et al., 1984). On an icy satellite, it is reasonable to expect this phenomenon to hold, especially since the cryomagma (water) is denser than the country rock (ice). Thus, we have proposed that while the ridge is being built on the

surface effectively as a cryoclastic fissure eruption (Kadel et al., 1998), a cryomagmatic sill
forms at a depth of ~1 km, at the level of neutral buoyancy of water in an ice shell (Fig. 3).

144 For the purposes of this work, these models may be assigned to different classes. Some of 145 these models are not consistent with the presence of the flanking fractures. The dike intrusion 146 model (Turtle et al., 1998), ice wedging model (Melosh and Turtle, 2004; Han and Melosh, 147 2010), and the compression model (Sullivan et al., 1998) predict local to regional compressive 148 stresses immediately exterior to the ridge, which would inhibit the formation of the fractures; 149 thus, we will not consider these models further. The cryovolcanic model of Kadel et al. (1998) 150 and the tidal squeezing model (Greenberg et al., 1998) have liquid water arising solely along the 151 pre-existing crack; we classify these mechanisms as "central conduit" models. Our cryovolcanic 152 sill variant (cf. Dombard et al., 2007) adds the thermal effects of a sill to the central conduit 153 models (Fig. 3). The wall diapir model (Head et al., 1999) is like the shear heating model 154 (Gaidos and Nimmo, 2000; Nimmo and Gaidos, 2002; Han and Showman, 2008) in that the 155 buoyancy that raises the ridge comes from thermal expansion due to heating along a vertical 156 plane in the ductile substrate that underlies the pre-existing crack in the brittle surface layer; thus we will consider these as one class that we will call "ductile heating." 157

Consequently, we will consider 3 classes: central conduit, cyrovolcanic sill, and ductile heating. Each class predicts a distinct thermal structure near the growing ridge, with a thermal anomaly overprinted on a background state. The flexure that we seek to simulate occurs in the lithosphere, which is the mechanical surface layer that can support stresses over geologic time. This layer is not pliable over tidal time scales, so any bulk tidal dissipation will occur deeper in the ice shell. Thus, the background thermal state is simply the conductive passage of heat generated within the interior of Europa (via tidal dissipation and decay of long-lived radioactive

165 nuclides in the silicate interior), with an expected surface heat flux in the range of several tens of mW m⁻² (see Schubert et al., 2004; Sotin et al., 2009). In the central conduit class, the pre-166 167 existing crack is filled with water very near its freezing point, and these temperatures will diffuse 168 into the surrounding ice. In addition to a central conduit thermal anomaly, the cryovolcanic sill 169 model proposes injection of a horizontal sheet of water near its freezing point, resulting in a 170 wider thermal anomaly than the central conduit models (Fig. 3). Last, the ductile heating models 171 predict localized heating in the ductile portion of the ice shell, strongest in the plane underneath 172 the pre-existing crack and decreasing with horizontal distance, resulting in a thermal anomaly 173 also wider than the central conduit models. We take the temperature field predicted in Nimmo 174 and Gaidos (2002) to be representative of this process.

175 **3. Measurements of Double Ridges**

176 Following Billings and Kattenhorn (2005), we compare the predicted lateral distance to peak 177 tensile flexural stresses from our simulations to the distances to fractures parallel to double 178 ridges. Thus, important constraints for our method are the distance to flanking fractures and the 179 half-width of the ridge. Billings and Kattenhorn (2005) identified flanking fractures associated 180 with 3 ridges on Europa: Androgeous Linea, Ridge C2r (Tufts et al., 1999), and Ridge R (Tufts 181 et al., 1999). Billings and Kattenhorn (2005) measured distances to fractures at 2-5 randomly 182 spaced locations along each ridge; in contrast, we measure ridge widths and the distance to 183 fractures at locations spaced 1 to 2 km apart along each ridge (20 measurements for ridge R and 184 30 for Androgeous Linea and Ridge C2r), determining an average value and a standard 185 deviation. All measurements were obtained from geo-referenced Galileo images. We have 186 examined all Galileo images with sufficient resolution to reveal these relatively fine scale 187 fractures, finding examples that flank a ridge in a region pervasively covered by multiple

generations of ridges (cf. Billings and Kattenhorn, 2005; Hurford et al., 2005). Thus, ridges with evidence of fracture are common but not abundant. Apart from the evidence of flexure, these ridges are morphologically similar to the other ridges in the image, which argues against them having formed from a different mechanism.

192 For Androgeous Linea, we find an average ridge half-width of 1.00 ± 0.11 km (one standard 193 deviation) and an average distance to fractures of 2.85 ± 0.17 km. For Ridge C2r, these 194 distances are 1.98 ± 0.23 km and 2.90 ± 0.25 km, and for Ridge R, they are 0.62 ± 0.07 km and 195 1.40 ± 0.19 km. Our measurements are comparable to past work. As demonstrated by the 196 relatively small standard deviations, the lateral distances to the flanking fractures remain fairly 197 constant over long distances for an individual ridge; however, there is significant variability 198 among ridges. Thus, we consider a lateral distance to the flanking fractures of 2 km but 199 recognize that any mechanism must explain distances between ~ 1 and ~ 3 km.

200 4. Finite Element Simulations

201 Our goal is to test which classes of formational models detailed in Section 2 are consistent 202 with observation of lithospheric flexure determined in Section 3. Specifically, we will examine 203 situations that are most favorable to flexure, in order to rule out those classes of models that 204 cannot result in any observable flexure for all reasonable situations. To investigate the 205 deformation of the lithosphere in the presence of these thermal anomalies, we use the 206 commercially available MSC.Marc finite element package, which we have used many times to 207 study the geodynamics of icy satellites (e.g., Dombard and McKinnon, 2000, 2006a, b; Dombard 208 et al., 2007; Kay and Dombard, 2011; Damptz and Dombard, 2011). We simulate a plane-strain 209 system, 5 km deep and 10 km wide, subdivided into 5000 quadrilateral elements (100 evenly 210 spaced elements horizontally and 50 elements vertically, with a bias to concentrate more

elements near the surface). The dimensions of the space and the resolution of the mesh are designed to impact negligibly the quality of our results (though we will discuss certain situations where the distance to the far side boundary may be an influence). The left side of the simulated space is assumed to be the central axis of the ridge system, so all boundary conditions there enforce symmetry. The process first involves a simulation of the thermal state, the results of which are imported into a mechanical simulation.

217 For the thermal simulation, we use the thermal conductivity of water ice of Klinger (1980). 218 which is inversely proportional to temperature. This conductivity is $\sim 15\%$ smaller than a later 219 version with the same functional form by Petrenko and Whitworth (1999), which is a simplified 220 fit to data from the same era as Klinger (circa 1980); however, lower conductivity translates into 221 higher thermal gradients for a given heat flux, which achieves our goal of testing conditions most 222 favorable to flexure. The surface temperature is locked at a constant value, usually 100 K (e.g., 223 Moore et al., 2009). The vertical sides of our finite element mesh are constrained to zero heat 224 flux, while a prescribed heat flux is applied to the bottom boundary. (Again, we assume any 225 bulk tidal dissipation occurs below the lithosphere.) Models of the thermal state of the ice shell of Europa usually predict a surface heat flux of a few tens of mW m^{-2} (e.g., Schubert et al., 2004; 226 227 Sotin et al., 2009); to create conditions most favorable to flexure, we usually implement a background heat flux at the higher end of this range of 40 mW m⁻². 228

The thermal anomalies are implemented by constraining the temperatures of the nodes (the corners of the quadrilateral elements) at the proper positions. For instance, simulation of the central conduit model involves constraining the nodes on the central axis to 270 K. The central axis nodes are also constrained for the sill model to 270 K, as well as a line of nodes 1 km deep out to a prescribed distance away from the central axis. For the ductile heating model, we digitize the anomalous temperature from Fig. 2d of Nimmo and Gaidos (2002), adding these
values to our background heat flow state. We then determine the steady-state solution to all
these conditions. We elect to investigate an equilibrium solution, as opposed to a transient
solution in which the domain heats or cools in response to application of the thermal anomalies,
because the steady-state solution will create the warmest conditions most favorable to flexure.

239 These thermal solutions are then input as an initial state into our mechanical simulations. 240 The rheology has 3 components: elastic (which ultimately provides the strength of the 241 lithosphere), viscous (to simulate temperature- and time-dependent ductile creep in ice), and 242 plastic (a continuum approximation of discrete brittle faulting). A direct consequence of this 243 multicomponent rheology is that the thickness of the lithosphere does not need to be input a 244 priori, but instead develops in response to the mechanical and thermal state of the system; in 245 addition, the adopted rheology also allows the lithosphere to evolve with time (see, e.g., Damptz 246 and Dombard, 2011). We assume the rheological properties of water ice, including the elastic 247 Young's modulus and Poisson's ratio from Gammon et al. (1983). For the ductile creep, we 248 employ a composite flow law that incorporates a dislocation creep mechanism and a grain-249 boundary diffusion creep mechanism acting in series with a grain-boundary sliding (GBS) 250 mechanism and a basal-slip mechanism that interact in a rate limiting sense (Goldsby and 251 Kohlstedt, 2001). Both the diffusion creep and GBS mechanisms are sensitive to the ice grain 252 size; following Dombard and McKinnon (2006a) who appealed to the analogy of terrestrial 253 glacial ice, we consider a range of grain sizes of 0.1-10 mm, with a nominal size of 1 mm. For 254 the plastic component, we use the results from ice friction experiments by Beeman et al. (1988).

A free-slip boundary condition is applied along the far side of the domain. Free-slip is also applied along the central (symmetry) axis of the ridge; while we could have adopted a "broken

plate" condition (see Turcotte and Schubert, 2002) due to the presence of the pre-existing crack 257 258 through the ice shell, mass continuity within the subsurface of Europa would enforce free-slip 259 conditions (i.e., no lateral displacements) under the central axis. We apply a Winkler-type, 260 buoyant restoring force on the bottom boundary. Coupled with an assumed mass density of 950 kg m⁻³, gravity with an acceleration of 1.35 m s⁻² is applied as a body force; because the 261 262 simulated material is compressible (i.e., elastic Poisson's ratio < 0.5), the application of gravity 263 requires the initial stress state be adjusted to lithostatic (vertical and horizontal stresses equal and 264 growing linearly with depth). The load imposed by the ridge is simulated as a series of elemental 265 surface pressures that step-wise approximate a 1.6 km wide (800 m half-width) and 240 m tall 266 symmetric ridge with a triangular cross-section. We linearly increase the magnitude of these 267 surface pressures, to approximate the growth of the ridge by deposition of material over a finite 268 time. Because double ridges are the most ubiquitous landform on Europa, we assume a growth 269 time of 100 kyr (enough for of order 100-1000 generations of ridges on Europa). A simulation 270 with the load instantly emplaced (zero growth time) produced negligibly different results, 271 demonstrating that the final deformation is insensitive to the growth time.

272 Although relative displacements and rotations are small (i.e., small strain conditions), we 273 implement a full large strain formalism, because it implicitly includes buoyant restoring forces 274 that arise from the displacement of density interfaces such as at the surface (cf. Turcotte and 275 Schubert, 2002). Additionally, a formalism is used that enforces constant dilatation across each 276 element, which prevents numerical errors that can arise in the simulation of nearly 277 incompressible behavior (e.g., ductile creep). Time stepping is automatically controlled to limit 278 everywhere in the mesh the creep strain increment to less than a quarter the elastic strain; this 279 algorithm effectively resolves the minimum viscoelastic Maxwell time by a factor of 4. To keep

280 the run times reasonable (~ 10 hr per simulation), we implement a minimum viscosity in the mesh 281 of 10^{19} Pa s (minimum Maxwell time of 90 yr), a value generally realized below the lithosphere. 282 Aspects of our results are sensitive to this artificial viscosity cut-off (e.g., time over which 283 flexure develops), but our main metric for simulation success (lateral distance to peak plastic 284 strain) is insensitive. Our measurements of double ridges show that the flanking fractures form 285 at a distance of 2 ± 1 km away from the central axis of the ridge. Thus, the primary metric that 286 we use to determine success or failure of our simulations is the horizontal distance on the surface 287 at which the lateral plastic strain peaks. We have confirmed that this peak is the principal tensile 288 strain, consistent with the formation of a flanking fracture, and we have confirmed that this 289 position is insensitive to the choice of the viscosity cut-off. The simulations are run past the 290 growth time (100 kyr) to 1 Myr, a time frame over which any thermal anomaly may still be 291 extant. All results are shown at this end time of 1 Myr.

292 5. Results

293 Most studies of ridge flexure on Europa do not appeal to local thermal anomalies but 294 implicitly assume a high regional heat flow (e.g., Billings and Katternhorn, 2005; Hurford et al., 295 2005). Thus, our first step is to determine the extent of lithospheric flexure under a uniform 296 background heat flow (no anomalies), in order to ascertain the magnitude that would be 297 necessary to produce the observed flanking fractures. A simulation with just a background heat flow of 40 mW m⁻² resulted in no appreciable flexure; the surface was deflected by only ~ 10 cm, 298 299 and the resulting stresses were insufficient to produce any plastic failure. The regional heat flow 300 would need to be significantly higher (more than an order of magnitude) to be consistent with the 301 observed fractures. Figure 4 shows the lateral distance to the peak plastic strain as a function of 302 the background heat flow value. Io-like heat flows are required. To put the flanking fractures at

3 km, a heat flow of \sim 700 mW m⁻² is needed (cf. Dombard et al., 2007). A heat flow of \sim 1-1.1 303 W m⁻² is needed for fractures at a distance of 2 km. The curve in Fig. 4 is well fit by a function 304 inversely proportional to the heat flow; for a lateral distance of 1 km, a heat flow > 2 W m⁻² is 305 needed. Figure 5 shows, for a heat flow of 1 W m^{-2} , a profile of the surface deflection and a 306 307 profile of the in-plane surface plastic strain (positive values indicate extension). The 308 contractional plastic strain near the axis would be underneath the ridge. The crest of the flexural 309 bulge (the subtle topographic high on the periphery of the central flexural trough) is at a lateral 310 distance of ~ 2.4 times the distance to the peak plastic strain. This finding suggests that for the 311 simulations near the lower end of the heat flow range in Fig. 4 (i.e., those with distances to peak 312 plastic strains of ~3 km or greater and thus bulge crests of at least 7-8 km distance), the far 313 boundary at 10 km distance may be interfering with the deformation, making the values in the 314 figure more suspect. However for a simulation with the mesh extended out to 20 km with a heat flow of 563 mW m⁻² (i.e., the case in Fig. 4 potentially most affected by this issue), the position 315 316 of peak plastic strain differs by < 3% (3.8 km vs. 3.7 km for the case with the far boundary at 10 317 km). Figure 5 also shows the deflection of an elastic plate under a line load (Section 3-16 in 318 Turcotte and Schubert, 2002), where the flexural bulge crests at the same distance from the 319 central axis as in our simulation (\sim 5.1 km) and the magnitude is scaled to match the depth on the 320 central axis. Using our material and planetary parameters, this elastic plate is ~ 140 m thick (cf. 321 Hurford et al., 2005). Maximum bending stresses (and hence the likely position of any brittle 322 failure) for this elastic plate occur at ~ 2.6 km from the central axis, slightly farther than in our 323 simulation. Differences are due to the different rheological models and to the fact that we 324 implement a distributed surface load.

325 Factors that enhance ductile creep allow for somewhat lower heat flow values. For a fracture 326 distance of 2 km (our typical value), the requisite heat flow in a simulation with a higher surface 327 temperature of 110 K (the average surface temperature at the equator is 106 K [Moore et al., 2009], compared to the 100 K we generally use) is lowered to closer to 800 mW m^{-2} (see Fig. 4). 328 329 For a simulation with a higher surface temperature and a grain size at the small end of our considered range (0.1 mm), a heat flow of between 600 and 700 mW m^{-2} is required. Even with 330 331 these enhancements, the regional heat flows needed to explain the flanking fractures are more 332 than an order of magnitude greater than the regional heat flows expected on Europa (see 333 Schubert et al., 2004; Sotin et al., 2009). Even estimates of maximum tidal dissipation in Europa vield maximum heat fluxes of 300-400 mW m⁻² (O'Brien et al., 2002; Hussmann and Spohn, 334 335 2004), far less than the values we predict here. This finding implicates a thermal anomaly in the 336 creation of the observed flexure.

337 The first class of thermal anomaly that we consider is the ductile heating model. The 338 application of the thermal anomaly from Nimmo and Gaidos (2002) on top of a background heat flow of 40 mW m⁻² results in almost as little flexure as the case with no anomaly (~30 cm vs. 339 340 ~ 10 cm of surface deflection, with no plastic strain). The anomaly digitized from Nimmo and 341 Gaidos (2002) used a brittle-ductile transition of 2 km depth; one might expect that a shallower 342 transition would squeeze the isotherms, producing a higher localized heat flow and more flexure. 343 When we cut the vertical (and horizontal) extent of the anomaly in half while keeping the same 344 excess temperatures however, the flexure is a bit less (~25 cm) because of the reduced horizontal 345 extent of the anomaly. Even cases that account for factors that enhance ductile creep (higher 346 surface temperature and smaller grain size) see negligible flexure (at most an increase in surface deflection of ~2.5 times and still no plastic strains). 347

348 Simulations testing central conduit models do result in plastic strain at the surface; however, 349 the failure is located very close to the central axis (within ~100 m, so therefore under the ridge 350 itself), where the thermal anomaly weakens the lithosphere the most. The plastic strain is also 351 negative, indicating contractional failure in a zone where the surface of the down-flexed 352 lithosphere is squeezed. Total vertical deformation is limited to ~ 2 m. Enhancing ductile creep 353 with a higher surface temperature and a smaller ice grain size results in ~21 m of total vertical 354 deformation; however, the displacements are concentrated near the central axis. At 800 m from 355 the axis (i.e., the edge of the ridge), the total displacement is < 7 m. The ductile-creep enhanced 356 case does experience a zone of extensional plastic failure, but it peaks at 600 m from the axis 357 (again, under the ridge itself). Like the ductile heating class, the central conduit class does not 358 result in deformation consistent with the flexure observed at double ridges. Even though peak 359 excess temperatures are higher and closer to the surface than in the ductile heating class, the 360 lateral extent of the thermal anomaly is too small to affect enough of the lithosphere. This 361 finding motivates a ridge formation model with a wider thermal anomaly.

362 Such widening is accomplished if a cryovolcanic sill is simulated by constraining the 363 temperature to 270 K of the nodes ~1 km deep to a certain distance away from the central axis. 364 This constraint produces a thermal anomaly, more laterally extended than the other classes, with a localized surface heat flow of 563 mW m⁻². The behavior of the system is more complex, 365 366 however, than simply considering a situation with a background heat flow of that value (see Fig. 4) or even a central conduit model with a background heat flow of 563 mW m^{-2} . The localized 367 368 thermal anomaly results in a relatively thin, weak lithosphere above the sill, transitioning into a 369 thick, very strong lithosphere at lateral distances beyond the sill. This squeezes the deformation into a smaller zone. The resultant plastic failure of the surface then depends on the lateral extent 370

of the sill (Fig. 6). For narrow sills, the peak plastic strain occurs near the edge of the sill, in the transition zone from thin to thick lithosphere at the edge of the thermal anomaly; however for sills wider than ~4 km from the central axis, peak plastic strains occur inward from this transition zone.

375 This change indicates 2 different behavioral regimes, which are shown in Fig. 7. The edge of 376 a sill with a half-width of 8 km is very near the lateral position of the crest of the flexural bulge for the case of simply a high regional heat flow of 563 mW m⁻² (at \sim 9.2 km). Thus, the 377 378 deformation associated with the localized thermal anomaly is squeezed into a smaller area than it 379 would be without the anomaly, concentrating the stresses and producing a general zone of plastic 380 failure over the entire anomaly. The deformation is not so squeezed, however, such that there 381 are still peak bending stresses (and hence plastic failure) at some point within this zone. For a much more narrow anomaly, the deformation is squeezed into such a narrow zone that stresses 382 383 are strongly concentrated right at the transition from thin to thick lithosphere. Between ~4 km 384 and \sim 5 km, there is a transition between these regimes.

In addition, the distance to the peak plastic strain is insensitive to differences in various parameters. Simulations with smaller regional heat flows, different (higher and lower) surface temperatures, and different (smaller and bigger) ice grain sizes still have peaks at the same distances as shown in Fig. 6. A somewhat counterintuitive result, this insensitivity arises because the system is less dependent on the thickness of the lithosphere and more dependent on the squeezing of the deformation into a narrower lateral zone.

6. Discussion and Conclusion

The central motivation of this work is to evaluate the models that have been proposed for the formation of double ridges on Europa on the basis of the observation of lithospheric flexure. Our

394 results indicate that nearly every model of ridge formation is inconsistent with the observed 395 flexure. If a ridge forms during an episode of very elevated, Io-like heat flow, the lithosphere 396 can flex appropriately, but given how ubiquitous ridges are on Europa, this elevated heat flow 397 state would have to be the norm. Consequently, it is likely that the flexure arises due to a locally 398 thin lithosphere that results from a thermal anomaly. The ductile heating model does not appear 399 to be consistent with the observation of flexure at double ridges on Europa, because the 400 magnitude of the anomaly and the spatial extent are too limited to affect sufficiently the 401 thickness of the lithosphere to permit the flexure. In fact, the situation is even more dire than our 402 results indicate, because a component of the ductile heating models (e.g., Head et al, 1999; 403 Nimmo and Gaidos, 2002) is that the ridge itself comes from the buoyancy of the thermal 404 anomaly, necessitating that the lithosphere deform on a horizontal scale of the width of the ridge 405 (kilometer scale), while our simulations show the lithosphere deforming on a much wider scale 406 (> 10 km). A variant of the shear heating model, developed to explain the plumes of icy particles 407 emanating from the south polar region of Enceladus (Nimmo et al., 2007), might be adapted to 408 explain the actual formation of a ridge as a surface build-up of erupted ice (a cryo-cinder pile), 409 thereby bypassing the requirement that the lithosphere deform on the scale of the width of the 410 ridge, but the thermal anomaly will still be too limited to explain the flexure. Similarly, the 411 central conduit models yield too narrow a thermal anomaly to explain the flexure. Furthermore 412 while models that propose regional compression are not seemingly consistent with the 413 interpretation that the flanking fractures are extensional in nature, we can gain insight from our 414 simulations. If anything, these models possess no anomaly or can be ascribed to the central 415 conduit class, which yields deformation (both elevation and horizontal scale) inconsistent with 416 double ridges.

417 Our simulations suggest that the injection of a cryovolcanic sill can produce a thermal 418 anomaly and a locally thin lithosphere that is consistent with the observation of flanking 419 fractures running parallel to double ridges. Indeed, the presence of intrusive cryomagmatism on 420 icy satellites is logical, because the magma is denser than the country rock and will reach a level 421 of neutral buoyancy before reaching the surface. Other researchers have also recognized this 422 possibility for Europa, speculating on the presence of sills ~1 km deep (Collins et al., 2000; 423 Manga and Wang, 2007). For a distance of 2 km from the central axis to the flanking fractures, 424 our results demonstrate the best match when the sill extends ~ 2.3 km from the central axis. 425 Emplacement of a sill would produce surface inflation comparable to the thickness of the sill 426 over a horizontal scale of 1-10 km (the width of the sill); however, surface deflections of this 427 magnitude may be difficult to observe, given currently available topographic data for Europa (e.g., Schenk, 2009). Europa has abundant topography at an amplitude of order 10 m, so while a 428 429 sill of order 100 m thick should yield observable surface inflation, a thinner sill (of order 10 m) 430 over such a long horizontal baseline would be largely invisible at present. On the other hand, our 431 simulations also show that the distance to the flanking fractures depends on the horizontal extent 432 of the sill. On a single ridge, the distance to the fractures does not vary significantly over the 433 tens of kilometers they are observed, and it is a challenge to envision a scenario in which the sill 434 maintains such a uniform width over such a long track. Furthermore, simple scaling of the 435 solidification of a sill (see Section 4-19 in Turcotte and Schubert, 2002) indicates a 10 m thick 436 sill will freeze in a matter of decades (using the ice parameters in Kirk and Stevenson, 1987). 437 This is too short a time (and too little excess heat) to affect strongly the overlying isotherms, 438 unless the central cryovolcanic conduit that feeds the growing ridge also replenishes hot water to 439 the sill. On the other hand, these issues might explain why ridges with evidence of flexure are

440 not abundant, because while it appears impossible to produce a ridge with the observed flexure 441 using other formational mechanisms, it may be straightforward to produce a ridge with this sill 442 model that lacks the observed flexure, depending on the local conditions. While the uniformity 443 of double ridges over long distances and the relatively short timescales for freezing of a sill 444 remain issues, our results indicate that only the cryovolcanic sill model is consistent with the 445 observed flexure.

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Figure 1. This high-resolution view of the Androgeos Linea double ridge (14.7 °N, 273.4 °W)
was taken by NASA's Galileo spacecraft during its E6 orbit. It is obvious that Androgeos Linea
is but the latest is a long history of double-ridge formation in this area. The arrows mark the
flanking, subparallel cracks.



Figure 2. This figure schematically reviews various models for double-ridge formation on
Europa. From Aydin (2006), which was adapted from Pappalardo et al. (1999) and Nimmo and
Gaidos (2002).



Figure 3. A cross-sectional schematic cartoon illustrating a model for a cryoclastically emplaced
double ridge, underlain by a cryomagmatic sill. The presence of the sill may heat the overlying
line, deflecting isotherms (dashed lines) upwards, locally thinning the lithosphere and thus
possibly explaining the flexure seen at some double ridges.



Figure 4. Lateral distance to peak plastic strain as a function of the background heat flow, for simulations without any thermal anomaly. The symbol size is coincident with the uncertainty, which is based off the mesh resolution of 100 m. The solid line is a fit to the cases with nominal parameters for Europa. The dash-dot line marks the situation of a higher surface temperature, while the dotted line marks the situation of a higher surface temperature and a smaller ice grain size. Io-like heat flows are needed to explain the flexure observed at double ridges, implicating a thermal anomaly in the creation of the flexure.



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Figure 5. Elevation profiles (left axis, solid lines) and a plastic strain profile (right axis, dashed line) as a function distance away from the central axis. The thick solid line is the elevation profile from our simulation, while the thin solid line is from a model of a thin (~140 m) elastic plate subjected to a line load and with a flexural bulge cresting at the same distance as our simulation results (~5.1 km). The dashed vertical line marks the distance to maximum bending stresses (i.e., the site of peak plastic strain) in this elastic plate model; this distance is somewhat farther from the central axis than that to the peak plastic strain in our simulation.



616 Figure 6. Lateral distance from the central axis to peak plastic strain as a function of sill half-617 width, for simulations testing the cryovolcanic sill model. The distance to peak plastic strain 618 scales roughly with the sill width for narrow sills, but plateaus at distances well within the edge 619 of the thermal anomaly for wide sills.



Figure 7. Profiles of lateral plastic strain as a function of surface distance away from the central axis, for simulations with sills of different widths. A zone of plastic strain over the thermal anomaly is seen for a case with a wide sill, with a peak in the plastic strain seen at distances well within the edge of the sill. On the other hand, plastic strains are strongly concentrated at the edge of the thermal anomaly for narrow sills. Sills of intermediate widths show transitional behavior.